

# Twin $H_4$ in quaternions, amalgamations and Iwahori-Matsumoto decompositions

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**Abstract.** We find two root systems of type  $H_4$  in quaternions. They create some infinite root system  $\Sigma$ . We will study it using amalgamations and Iwahori-Matsumoto decompositions.

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